

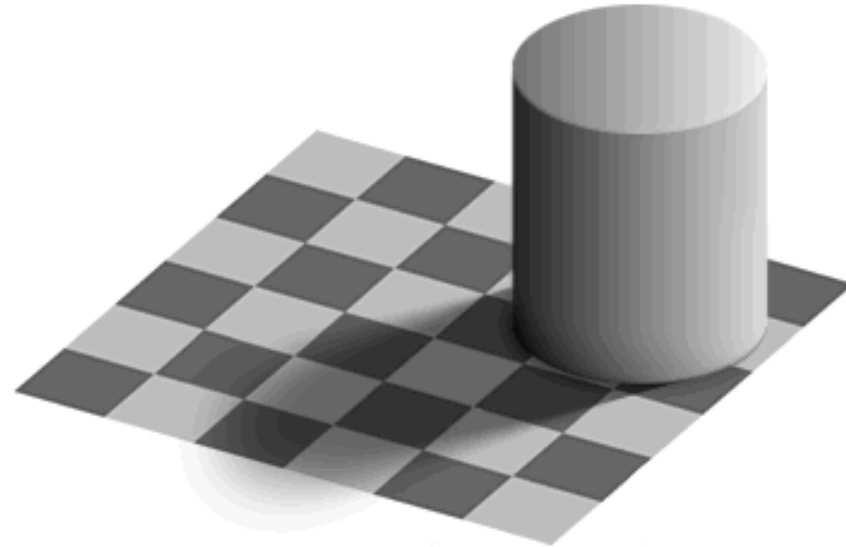


# *COSC579: Radiometry*

Jeremy Bolton, PhD  
Assistant Teaching Professor

A special thanks to professors and researchers professor and researchers Yung-Yu Chuang, Fredo Durand, Alexei Efros, William Freeman, James Hays, Svetlana Lazebnik, Andrej Karpathy, Fei-Fei Li, Srinivasa Narasimhan, Silvio Savarese, Steve Seitz, Noah Snavely, Richard Szeliski, and Li Zhang.

# *Light*



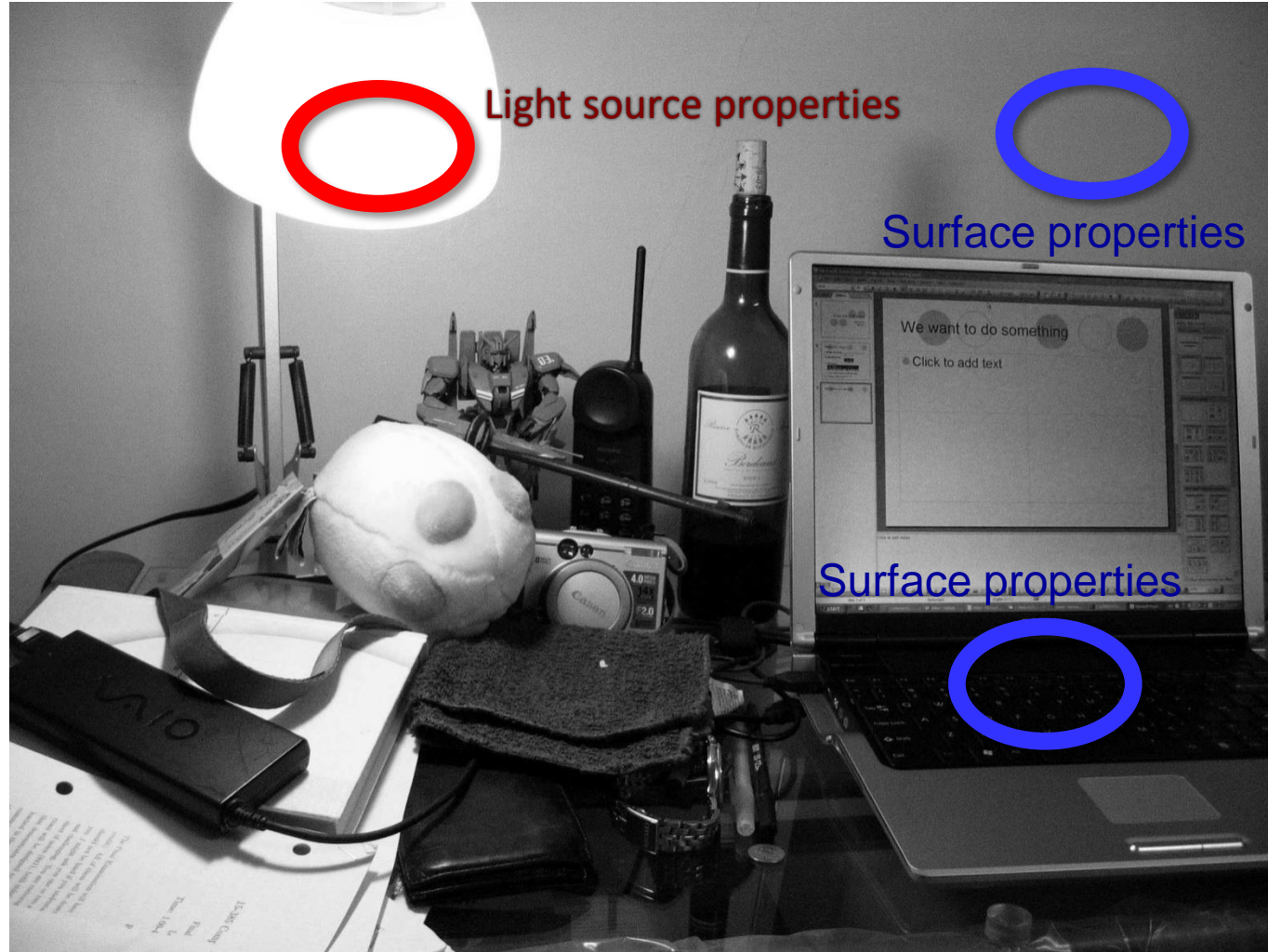
- Readings
  - Szeliski, 2.2, 2.3.2

# *Properties of light*

- Today
  - What is light?
  - How do we measure it?
  - How does light propagate?
  - How does light interact with matter?

# Radiometry

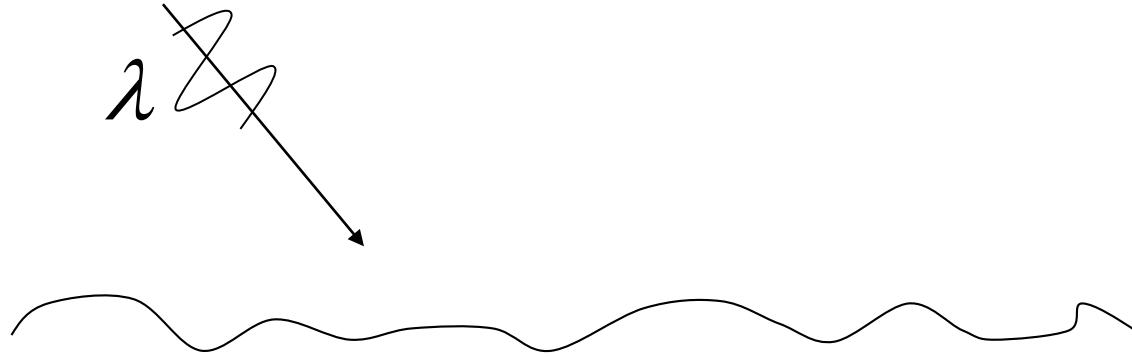
- What determines the brightness of an image pixel?



# Reflectance Models

---

Reflection: An Electromagnetic Phenomenon



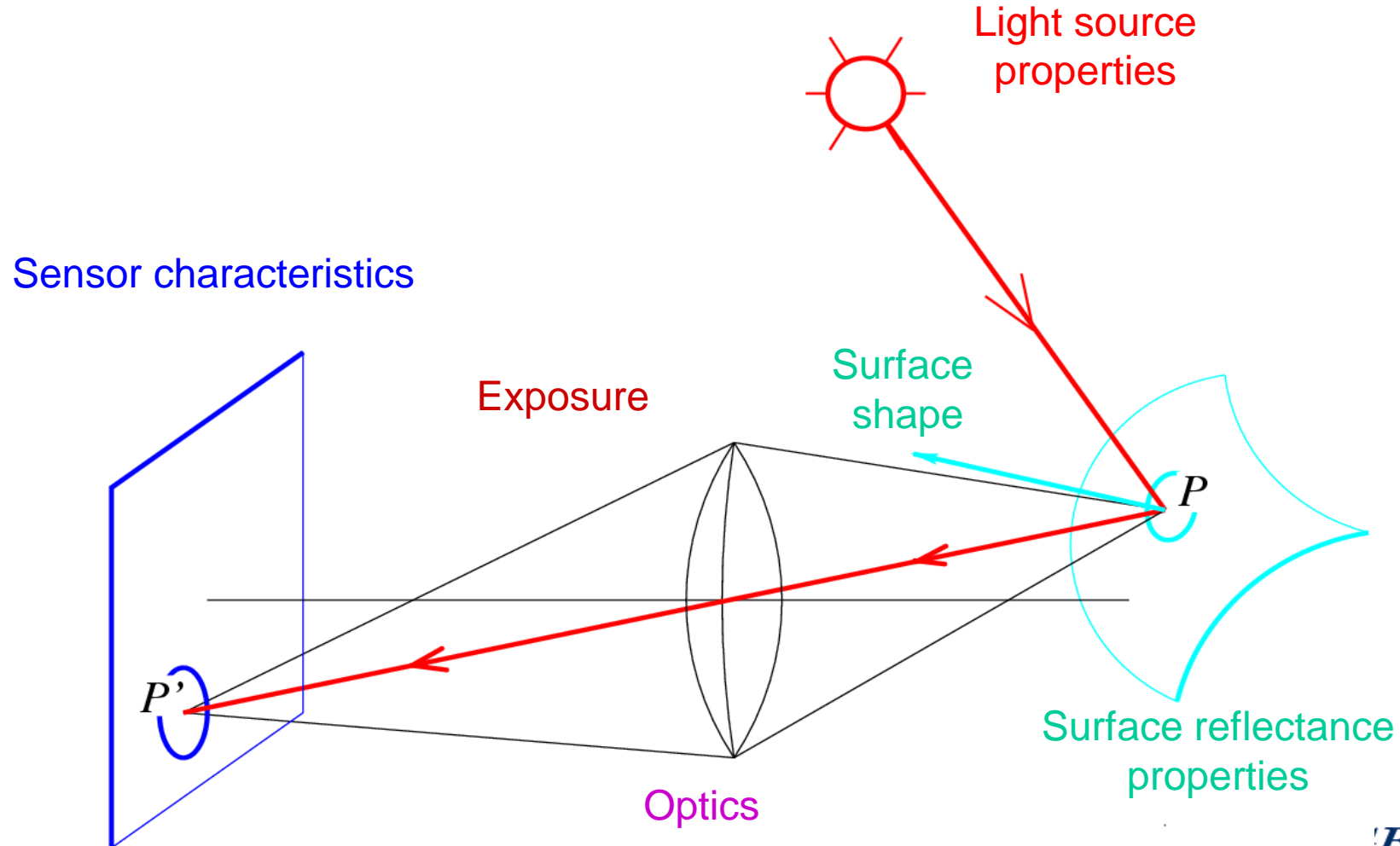
Two approaches to derive Reflectance Models:

- Physical Optics (Wave Optics)
- Geometrical Optics (Ray Optics)

Geometrical models are approximations to physical models  
But they are easier to use!

# Radiometry

- What determines the brightness of an image pixel?



# *What is light?*

Electromagnetic radiation (EMR) moving along rays in space

- Radiance  $L(\lambda)$  is EMR, measured in units of power (watts)
  - $\lambda$  is wavelength

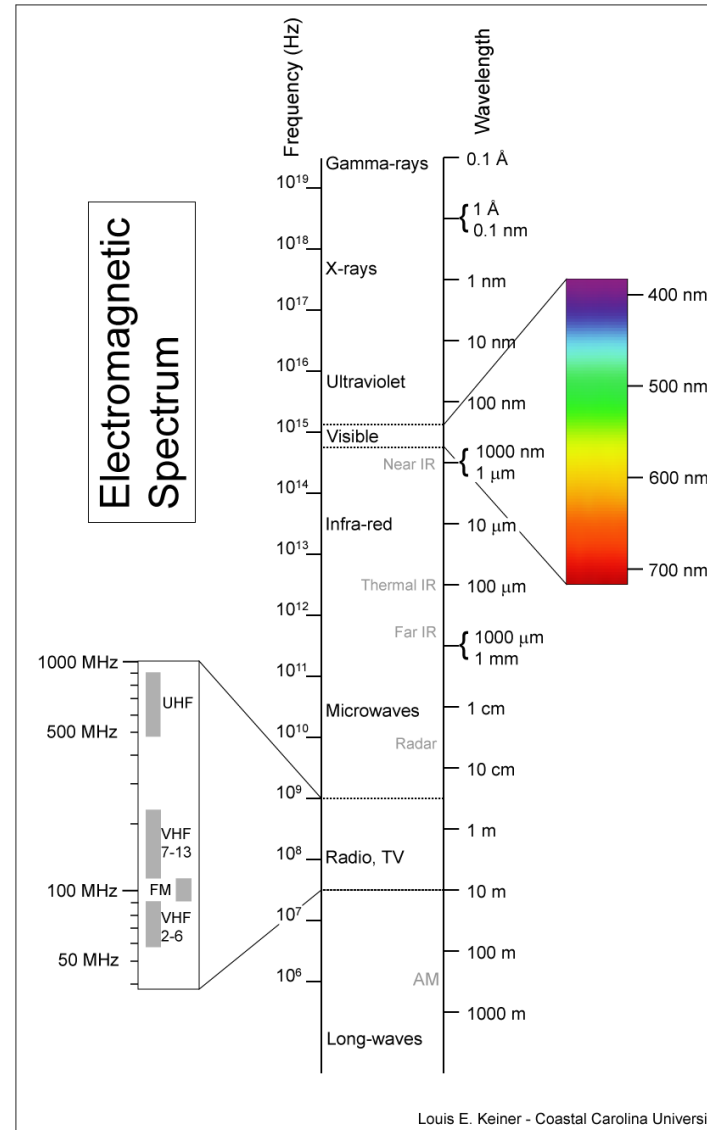


Perceiving light

- How do we convert radiation into “color”?
- What part of the spectrum do we see?

# Visible light

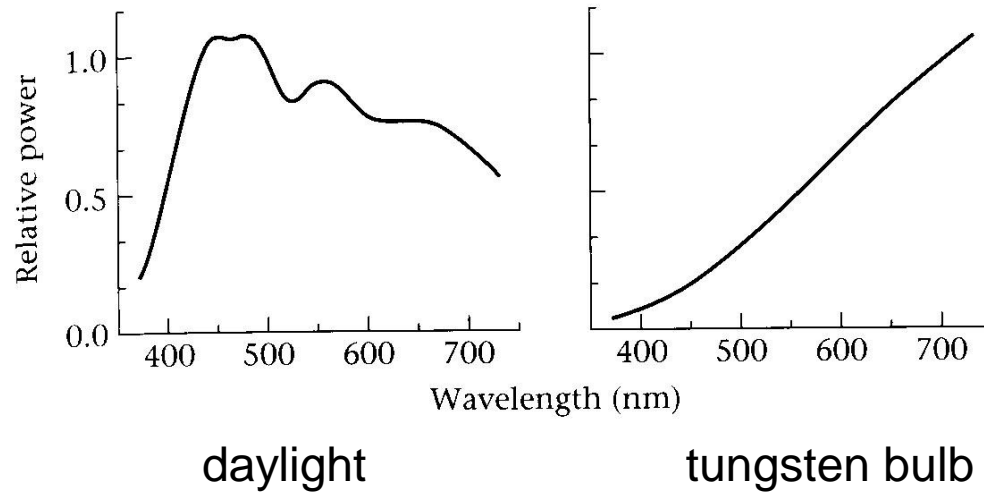
- We “see” electromagnetic radiation in a range of wavelengths





# *Light spectrum*

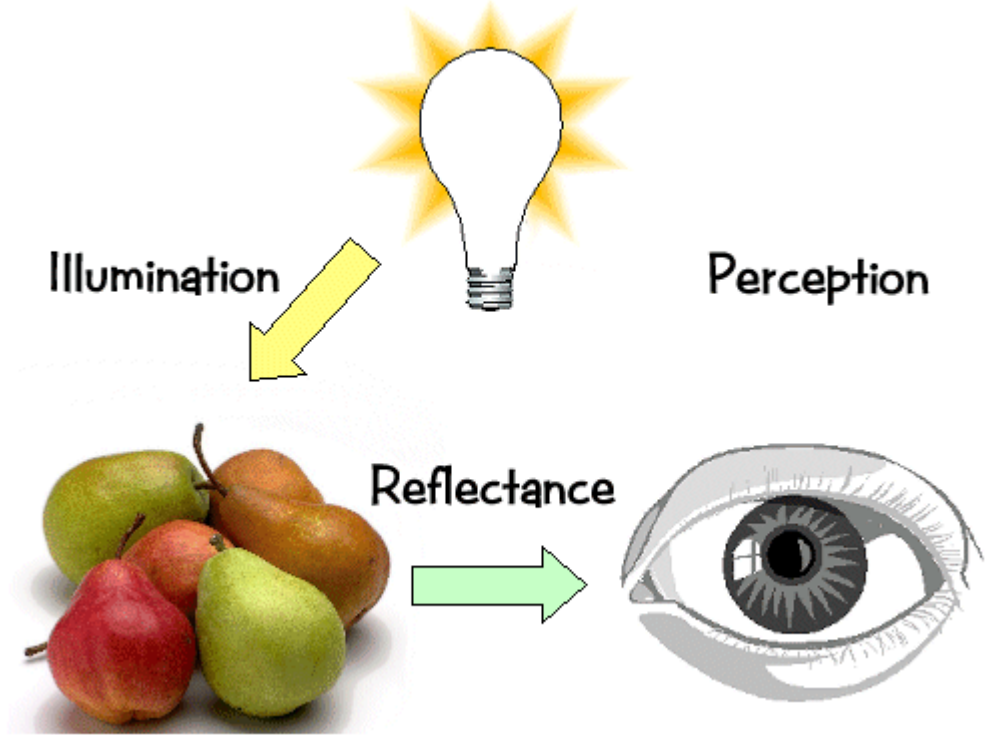
- The appearance of light depends on its power **spectrum**
  - How much power (or energy) at each wavelength



Our visual system converts a light spectrum into “color”

- This is a rather complex transformation

# *Light transport*



# *Light sources*

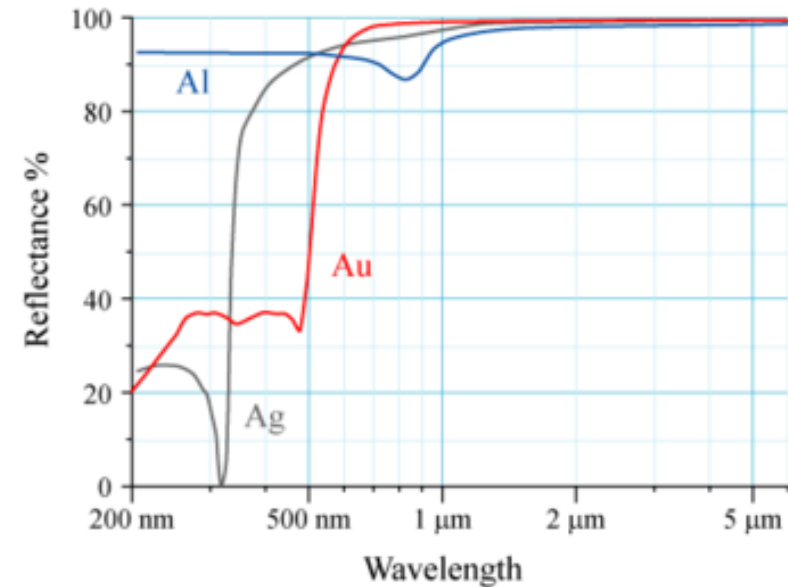
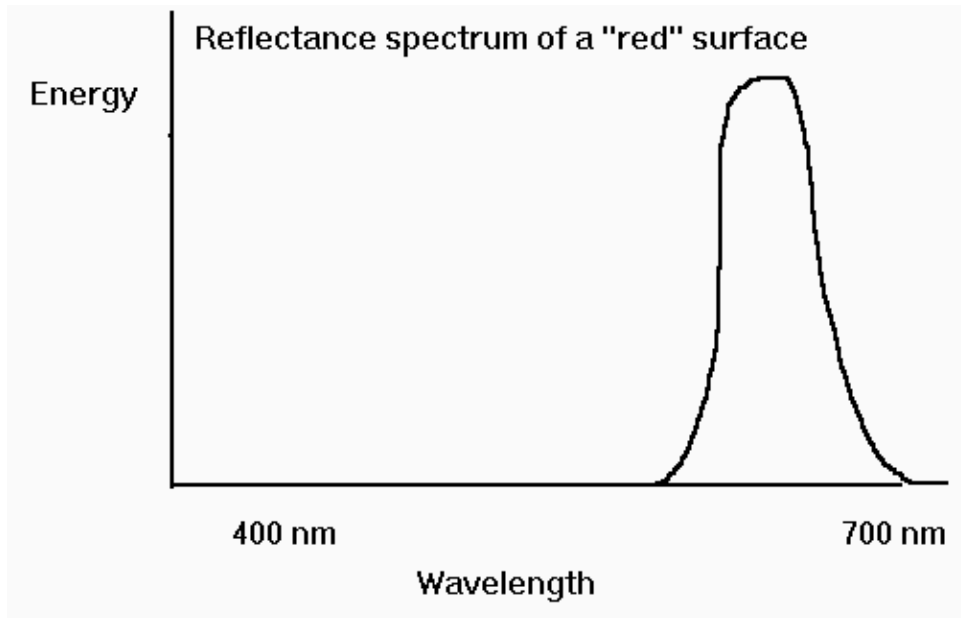
- Basic types
  - point source
  - directional source
    - a point source that is infinitely far away
  - area source
    - a union of point sources
- More generally
  - a light field can describe *\*any\** distribution of light sources
- What happens when light hits an object?

# *What happens when a light ray hits an object?*

- Some of the light gets absorbed
  - converted to other forms of energy (e.g., heat)
- Some gets transmitted through the object
  - possibly bent, through “refraction”
  - a transmitted ray could possible bounce back
- Some gets reflected
  - as we saw before, it could be reflected in multiple directions (possibly all directions) at once
- Let’s consider the case of reflection in detail

# Reflectance spectrum (*albedo*)

- To a first approximation, surfaces absorb some wavelengths of light and reflect others

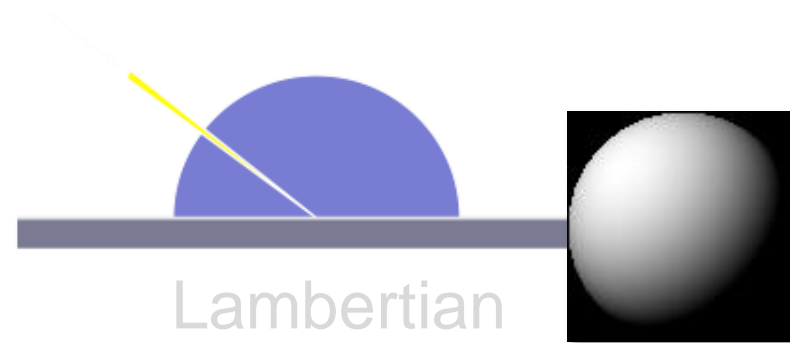
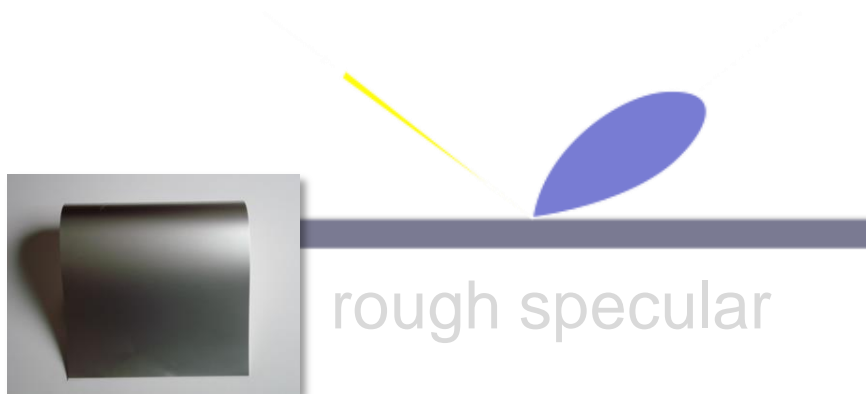
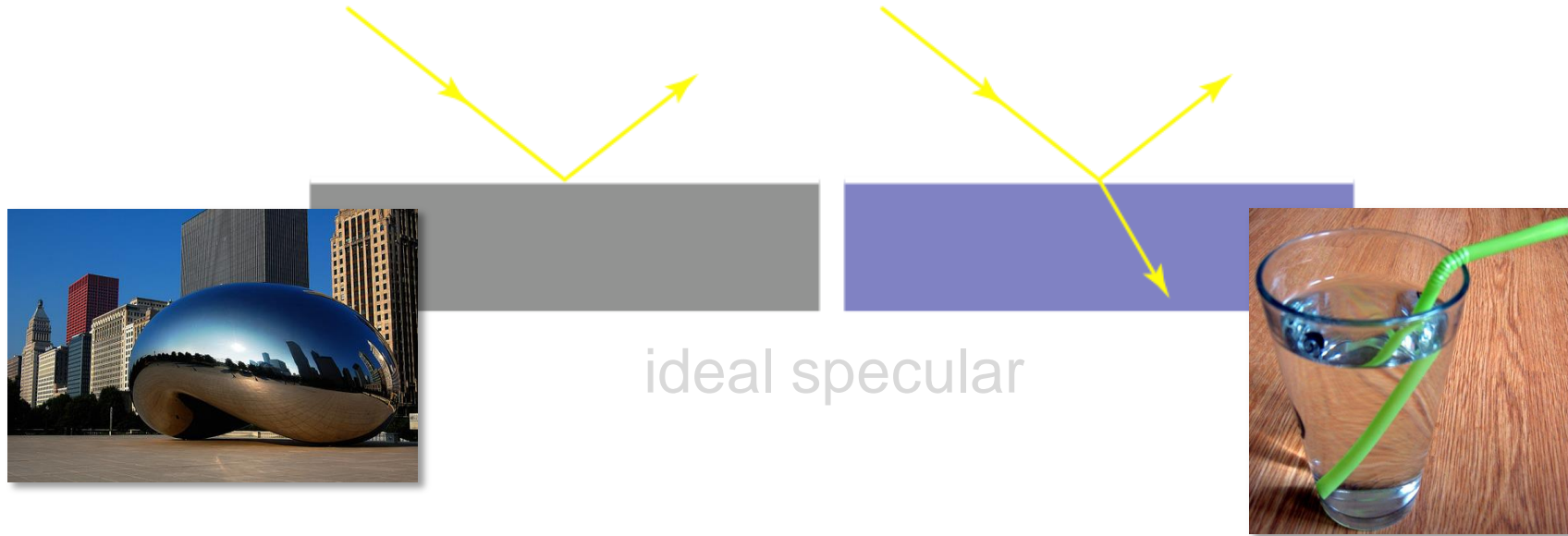


- These spectra are multiplied by the spectra of the incoming light, then by the spectra of the sensors

# *Material Properties*

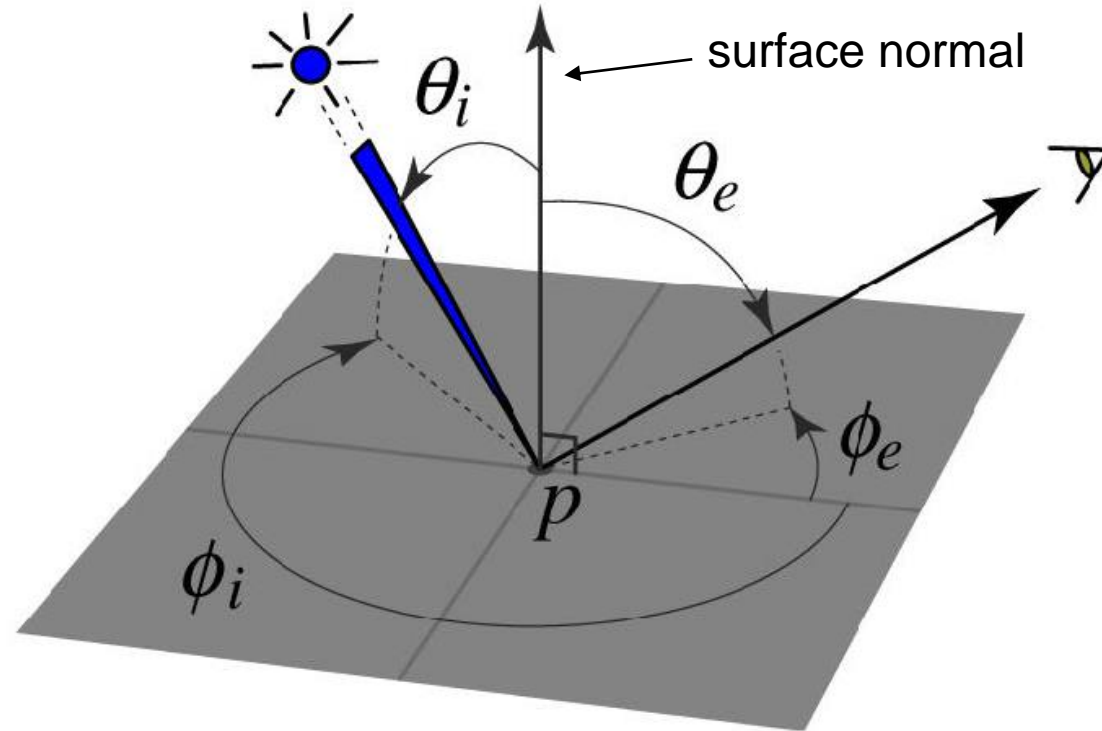


# Classic reflection behavior



# The BRDF

- The Bidirectional Reflection Distribution Function
  - Given an incoming ray  $(\theta_i, \phi_i)$  and outgoing ray  $(\theta_e, \phi_e)$   
what proportion of the incoming light is reflected along outgoing ray?

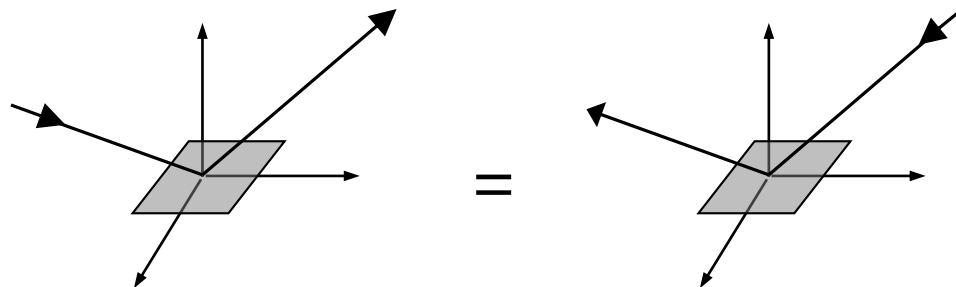


Answer given by the BRDF:  $\rho(\theta_i, \phi_i, \theta_e, \phi_e)$



# *Constraints on the BRDF*

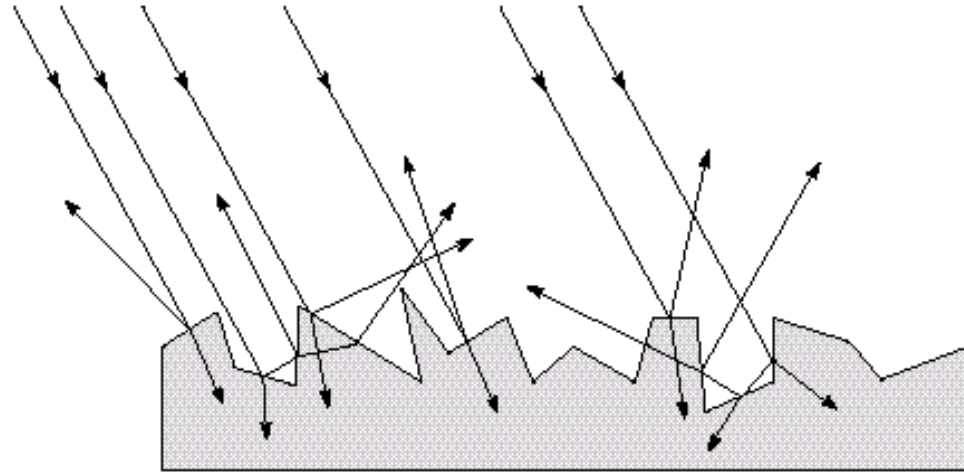
- Energy conservation
  - Quantity of outgoing light  $\leq$  quantity of incident light
    - integral of BRDF  $\leq 1$
- Helmholtz reciprocity
  - reversing the path of light produces the same reflectance



*BRDF's can be incredibly complicated...*



# *Diffuse reflection*

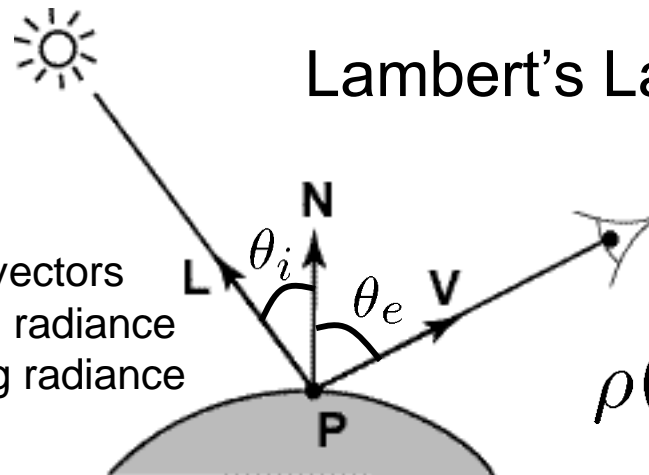
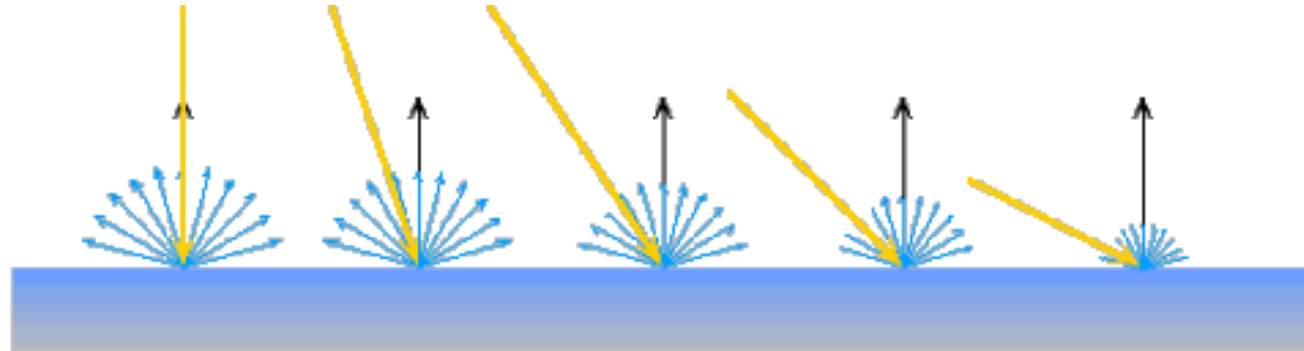


- Diffuse reflection
  - Dull, matte surfaces like chalk or latex paint
  - Microfacets scatter incoming light randomly
  - Effect is that light is reflected equally in all directions

# Diffuse reflection

Diffuse reflection governed by **Lambert's law**

- Viewed brightness does not depend on viewing direction
- Brightness *does* depend on direction of illumination
- This is the model most often used in computer vision



Lambert's Law:  $I_e = k_d \mathbf{N} \cdot \mathbf{L} I_i$

$k_d$  is called **albedo**

BRDF for **Lambertian surface**

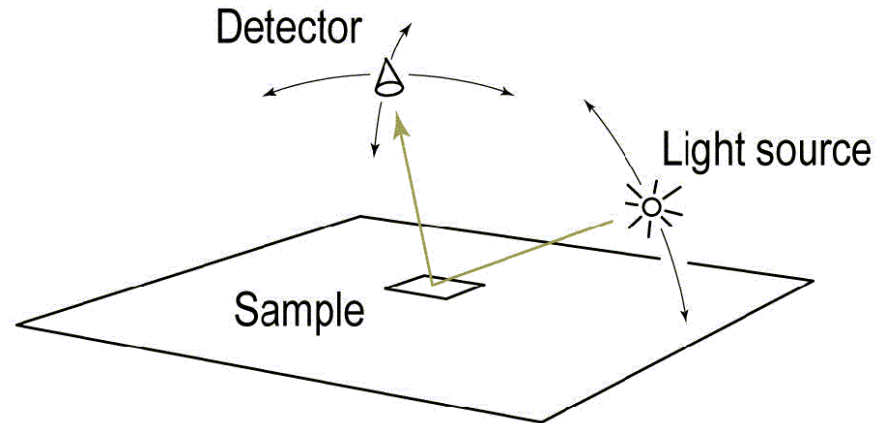
$$\rho(\theta_i, \phi_i, \theta_e, \phi_e) = k_d \cos \theta_i$$

$\mathbf{L}$ ,  $\mathbf{N}$ ,  $\mathbf{V}$  unit vectors  
 $I_e$  = outgoing radiance  
 $I_i$  = incoming radiance

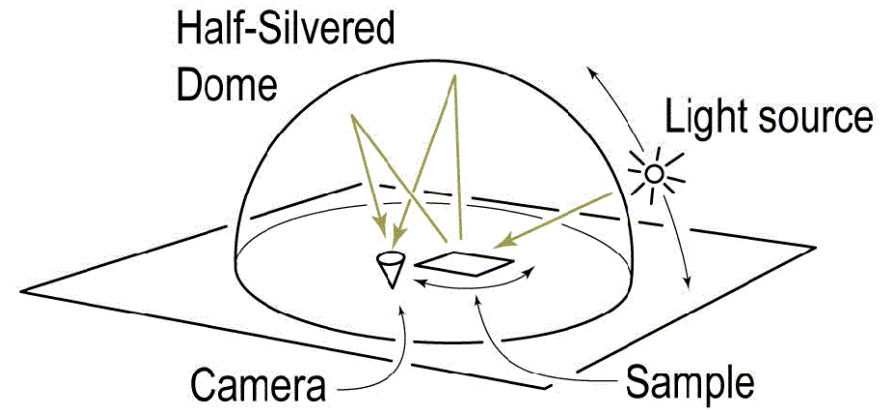
# *BRDF models*

- Phenomenological
  - Phong [75]
  - Ward [92]
  - Lafortune et al. [97]
  - Ashikhmin et al. [00]
- Physical
  - Cook-Torrance [81]
  - Dichromatic [Shafer 85]
  - He et al. [91]
- Here we're listing only some well-known examples

# Measuring the BRDF



traditional



design by Greg Ward

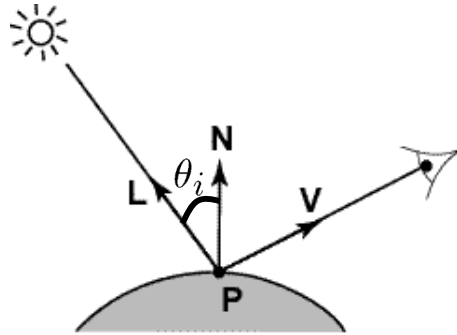
- Gonioreflectometer
  - Device for capturing the BRDF by moving a camera + light source
  - Need careful control of illumination, environment

# *Why models for light?*

- Why model these complex processes?
- Vision is all about extracting information about a scene from its 2-d representation
  - Shape from shading
  - Surface Properties
  - Texture Features
  - Information from reflections
  - Atmosphere

# Shape from shading

- Suppose  $k_d = 1$



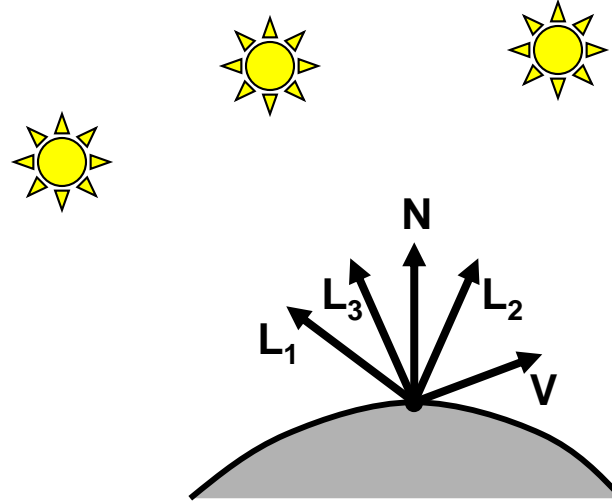
$$\begin{aligned} I &= k_d \mathbf{N} \cdot \mathbf{L} \\ &= \mathbf{N} \cdot \mathbf{L} \\ &= \cos \theta_i \end{aligned}$$

You can directly measure angle between normal and light source

- Not quite enough information to compute surface shape
- But can be if you add some additional info, for example
  - assume a few of the normals are known (e.g., along silhouette)
  - constraints on neighboring normals—“integrability”
  - smoothness
- Hard to get it to work well in practice



# *Photometric stereo: for estimating surface normal (shape!)*



$$I_1 = k_d \mathbf{N} \cdot \mathbf{L}_1$$

$$I_2 = k_d \mathbf{N} \cdot \mathbf{L}_2$$

$$I_3 = k_d \mathbf{N} \cdot \mathbf{L}_3$$

Can write this as a matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = k_d \begin{bmatrix} \mathbf{L}_1^T \\ \mathbf{L}_2^T \\ \mathbf{L}_3^T \end{bmatrix} \mathbf{N}$$

# *Light and Shadows*



*GEORGETOWN*  
*UNIVERSITY*





# *Reflections*







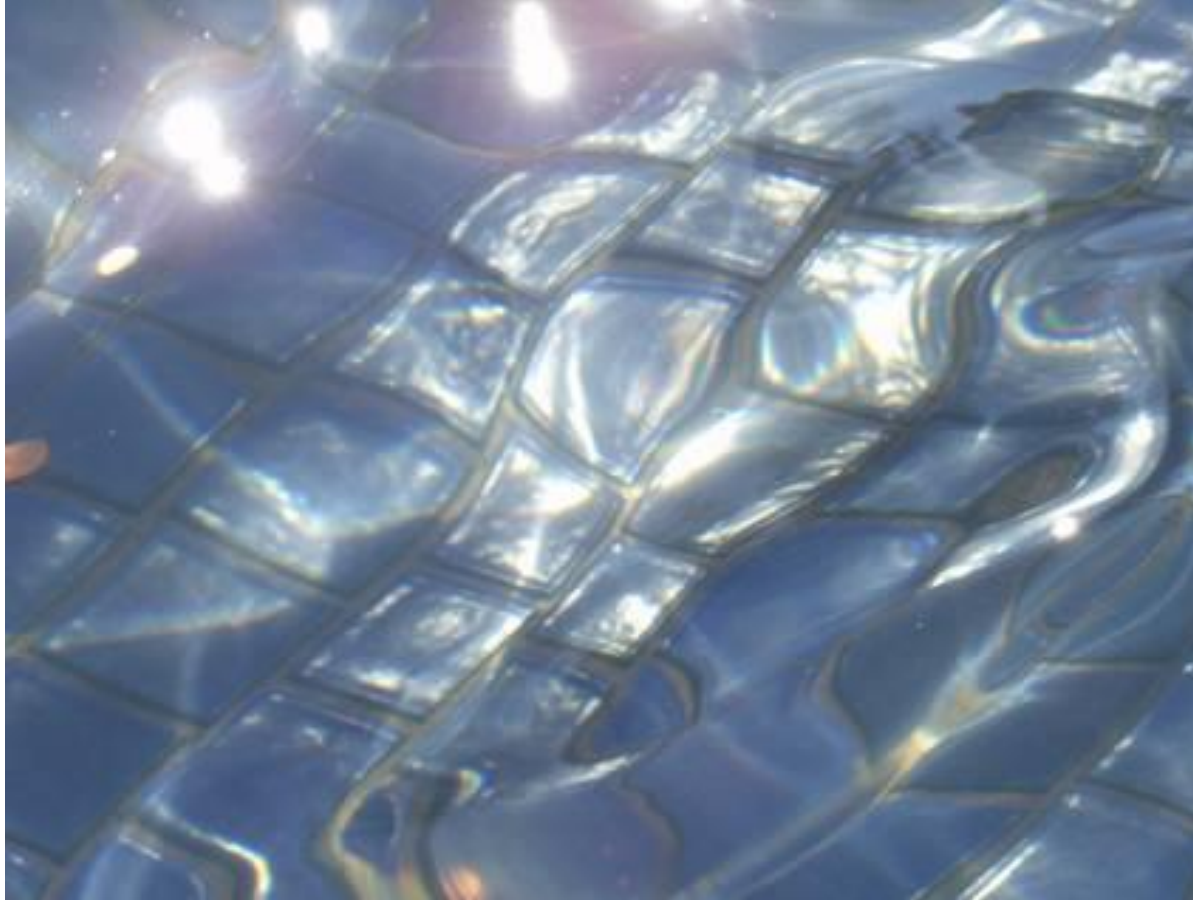




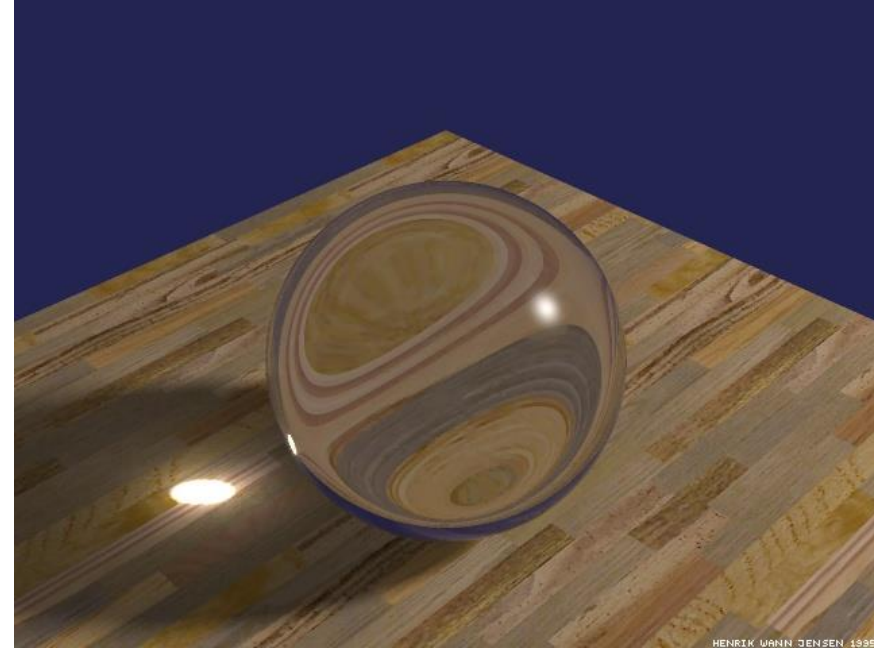




# *Refractions*









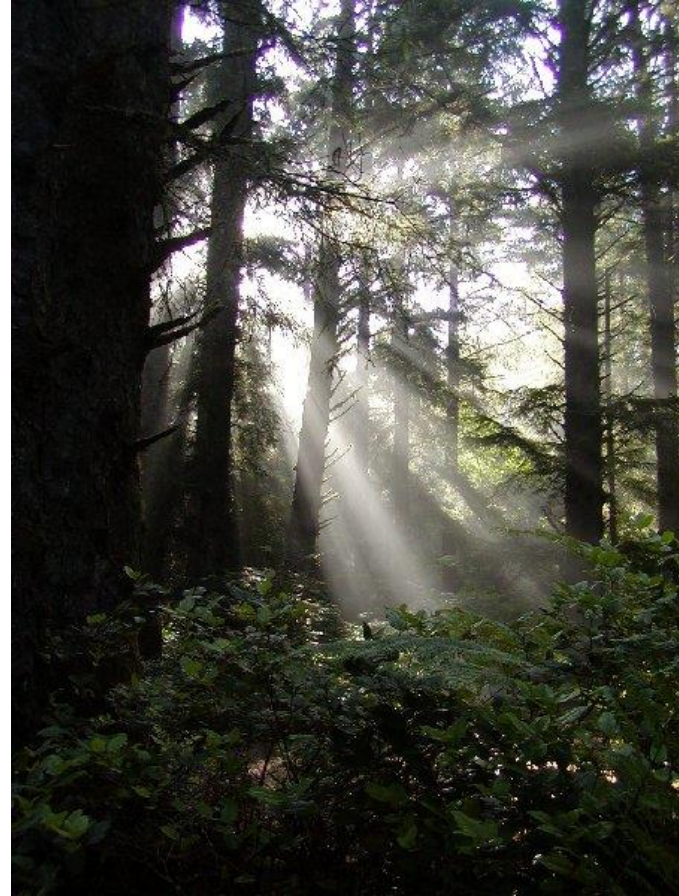


# *Interreflections*

Mies Courtyard House with Curved Elements



# *Scattering*







Haze



De-hazed













# *More Complex Appearances*











## *Appendix: Measuring Light*

Jeremy Bolton, PhD

Assistant Teaching Professor

A special thanks to many contributors over the years: Szeliski, Snavely, Adelson

GEORGETOWN  
UNIVERSITY